

## slln-lemma2<sup>11,40</sup>

$\forall p:\text{FinProbSpace}, f:(\mathbb{N} \rightarrow \mathbb{N}), X:(n:\mathbb{N} \rightarrow \text{RandomVariable}(p;f(n))), s, k:\mathbb{Q}.$   
 $(\forall n:\mathbb{N}, i:\{0..n^-\}. f(i) < f(n))$   
 $\Rightarrow (\forall n:\mathbb{N}.$   
 $E(f(n);X(n)) = 0 \in \mathbb{Q}$   
 $\& E(f(n);(x.x * x) o X(n)) = s$   
 $\& E(f(n);(x.(x * x) * x * x) o X(n)) = k)$   
 $\Rightarrow (\forall n:\mathbb{N}, i:\{0..n^-\}. \text{rv-disjoint}(p;f(n);X(i);X(n)))$   
 $\Rightarrow (\exists B:\mathbb{Q}$   
 $\quad (\forall n:\mathbb{N}.$   
 $\quad E(f(n);\text{rv-partial-sum}(n;k.\text{if } (k =_0 0)$   
 $\quad \text{then } 0$   
 $\quad \text{else } (x.(x * x) * x * x) o (1/k)*\text{rv-partial-sum}(k;i.X(i))$   
 $\quad \text{fi })) \leq B))$